

Role of grain-size in phyllonitisation: Insights from mineralogy, microstructures, strain analyses and numerical modeling

Narayan Bose, Dripta Dutta, Soumyajit Mukherjee*

Department of Earth Sciences, Indian Institute of Technology Bombay, Powai, Mumbai, 400 076, Maharashtra, India



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ABSTRACT

Brittle Y- and P-planes exist in an exposure of greywacke in the Garhwal Lesser Himalaya, India. Although, Y-planes are well developed throughout, the P-planes are prominent only in some parts (domain-A), and not elsewhere (domain-B). To investigate why the P-planes developed selectively, the following studies were undertaken: 1. Clay-separated XRD analyses: clinocllore and illite are present in both the domains. 2. Strain analyses by R_f - ϕ method: it deduces strain magnitudes of ~ 1.8 for the ductile deformed quartz grains from both the domains A and B. 3. Grain size analyses of quartz clasts: domain-A is mostly composed of finer grains (area up to $40,000 \mu\text{m}^2$), whereas domain-B consists of a population of coarser grains (area $> 45,000 \mu\text{m}^2$). A 2D finite element modeling of linear elastic material was performed using COMSOL software to investigate the control of grain-size variation on the generation brittle shear planes. The results of numerical modeling corroborate the known fact that an increase in grain-size reduces the elastic strain energy density. A broader grain-size distribution increases the effects of diffusion creep and resists the onset of dislocation creep. Thus, rocks with coarser grain population (domain B) tend to resist the generation of shear fractures, unlike their fine-grained counterpart (domain A).

1. Introduction

Brittle shear tectonics has far-reaching implications in dynamic rupturing during earthquakes (Harris et al., 1991), in petroleum geosciences (Fjar et al., 2008) and in CO₂ sequestration (Cappa and Rutqvist, 2011). Brittle failure due to shear, which usually occurs at the upper crustal levels, produces several kinds of fractures, viz. Y, P, R etc. (Bartlett et al., 1981; Passchier and Trouw, 2005). Shear fractures preferably develop in the less competent zones (Treagus, 1988; Marinho and Gomes, 2013) undergoing higher strain (Kanagawa, 1993). Tang et al. (2000) reported that tensile fractures generated in a shear band leads to faulting. In nature, there may be insignificant movement along the shear fractures due to profound stress drop during fracturing (Mandl, 1999). Moreover, shearing produces hybrid fracture (Ramsey and Chester, 2004; Peacock et al., 2018), rather than a typical shear- or a tensile-fracture. Gudmundsson (2011) defines fractures and other brittle planes as mechanical discontinuities in the rock across which cohesion drops. Both shear- and normal-stress can be responsible for the failure. The author further asserts that, unlike the fracture surfaces, their tips do exhibit evidences of ductile deformation, and that fracture propagation does involve plasticity. Brittle shear zones may possess deformation markers, which are discontinuous across the shear

fractures (Fossen and Cavalcante, 2017). Y- and P- planes are shear fractures (or shear joints), and are useful to decipher the shear sense (Passchier and Trouw, 2005; Peacock et al., 2016). The angle between Y- and P- plane can range from 10 to 45° (Meyer et al., 2017).

Experimental studies indicate that, as stress increases, material in general deforms elastically, till the elastic limit, followed by plastic deformation. During elastic deformation the strain energy is stored and can be used to regain the initial shape. On the other hand, in plastic deformation, the energy is consumed in the shape change (plastic elongation). Various lab experiments show that, under a constant strain rate, fine-grained rocks attain plasticity much earlier than the coarse-grained ones (e.g., Karato et al., 1986). Hence, plastic deformation is expected to be more ubiquitous in the former. Moreover, the yield stress tends to decrease with increase in grain size for n (stress exponent) > 2 (Twiss and Moores, 2007). For both dry and wet quartzites, $n = 2.72 \pm 0.19$ (Koch et al., 1989). Quartz grains deformed under dislocation creep regime have $n \sim 3$ to 4 (Luan and Paterson, 1992; Gleason and Tullis, 1995; Rutter and Brodie, 2004). Morales et al. (2011) however, reported a wider range of n for quartzites: 1.4–5.7 with 2.75 as the mean value. Close to the brittle-ductile transition zone $n = 5$ (Fukuda and Shimizu, 2017 and references therein).

During brittle deformation grain-size reduces by brittle fracturing

* Corresponding author.

E-mail addresses: narayan.bghs@gmail.com (N. Bose), dripta.dutta@gmail.com (D. Dutta), soumyajitm@gmail.com (S. Mukherjee).

(cataclasis; Passchier and Trouw, 2005). This may happen in several steps (Keulen et al., 2007) by recrystallization that perturbs the effect of stress on individual grains (TerHeege et al., 2002). This is true especially for quartz grains (Gueydan et al., 2005), where additionally secondary minerals precipitate during mylonite to ultramylonite transition (Kilian et al., 2011). However, the size of the recrystallised quartz grains is temperature-independent and remains unchanged after the nucleation process (Xia and Platt, 2018).

This work aims to check the effects of grain size in natural deformation. Y-planes are present throughout the studied rock exposure in the Lesser Himalaya, but P-fractures occur locally. From field observations, microstructural studies and numerical modeling, we investigate the mechanisms and controlling factors for the selective generation of P-planes. Mineralogical and microstructural studies were followed by strain- and grain size analyses. The results, thus obtained, were used in numerical modeling.

2. Geology

The study area is located at the Inner-Lesser Himalaya of the Uttarakhand district, India. The Proterozoic sedimentary rocks (greywacke/quartz arenite) present here belong to the Rautgara Formation (Fig. 1; Valdiya, 1980, 2010; C  lerier et al., 2009; Dubey, 2014). These rocks have also been reported as the Netala Quartzite (Jain, 1971; Agarwal and Kumar, 1973). The grade of metamorphism is very low and it increases up to greenschist near the Main Central Thrust (MCT) zone towards N (e.g. Thakur, 1992; Metcalfe, 1993). The Munsiri Thrust, which is also the northern boundary of the Lesser Himalaya and the southern boundary of the MCT zone, is ~20 km E from the study location. The rocks have undergone two deformation phases (Agarwal and Kumar, 1973; Thakur and Kumar, 1994): *D1*- NE-SW compression that produced NW-SE trending folds (F_1 ; such as, Baragadi, Netala, Sialamgad Anticlines in Fig. 1) and axial planar faults (e.g. the Gangori-Jamak Fault), followed by *D2*- NW-SE compression that gave rise to ~ NE-SW trending folds (F_2). However, Pant et al. (2012) claimed that F_2 folds developed prior to F_1 . The rare-earth-element studies and

palaeo-current directions of the Rautgara Formation indicate its provenance in the Archean Aravalli-and Bundelkhand granitoids (Rashid, 2005; McKenzie et al., 2011).

3. Deformation structures and sample description

3.1. Outcrop-scale structures

The N-trending rock exposure (30 45.114'N, 78 27.189'E) is located ~3 km N of Uttarkashi along the Bhagirathi river section, Uttarakhand state, India. The near-vertical exposure of the rock is devoid of any meso-scale folding and ductile shear-sense indicators (Fig. 2a). Instead, it is brittle sheared, and we designate this as the ‘‘Gangori Shear Zone’’. Based on the presence of brittle Y- and P-planes, two domains were distinguished in the outcrop: 1. Domain A (Fig. 2a') - where both the Y- and the P- planes are present, 2. Domain B (Fig. 2b') - where only Y-plane is present and the P-plane is absent mesoscopically. The Y-planes in both these domains dip ~ SW. The shear sense deciphered from the P-planes is ‘top-to-SW (down) extensional’ i.e., normal fault like shear. Oriented samples were collected from domains-A and B.

3.2. Petrography of samples

The matrix content ranges 15–75% (by volume) and the framework is mostly quartz, along with few calcite (Fig. 3). Hence, as per Pettijohn's scheme (Pettijohn, 1984), rocks from domains A and B are greywacke. X-ray diffraction (XRD) analyses were performed on samples from domains A and B using the PANalytical Empyrean (PANalytical B.V., Almelo, The Netherlands) setup at IIT Bombay. The powdered (< 75  m) samples were taken through decantation and centrifuge processes to separate the silts from clays. Then the air dried samples were studied followed by ethylene glycol (vapour) treatment. The reader can consult other articles (e.g., Moore and Reynolds, 1989; Poppe et al., 2001) for details of XRD studies. XRD results were analysed using the HighScore Plus software and the Inorganic Crystal Structure Database (ICSD). The samples from domains A and B consist

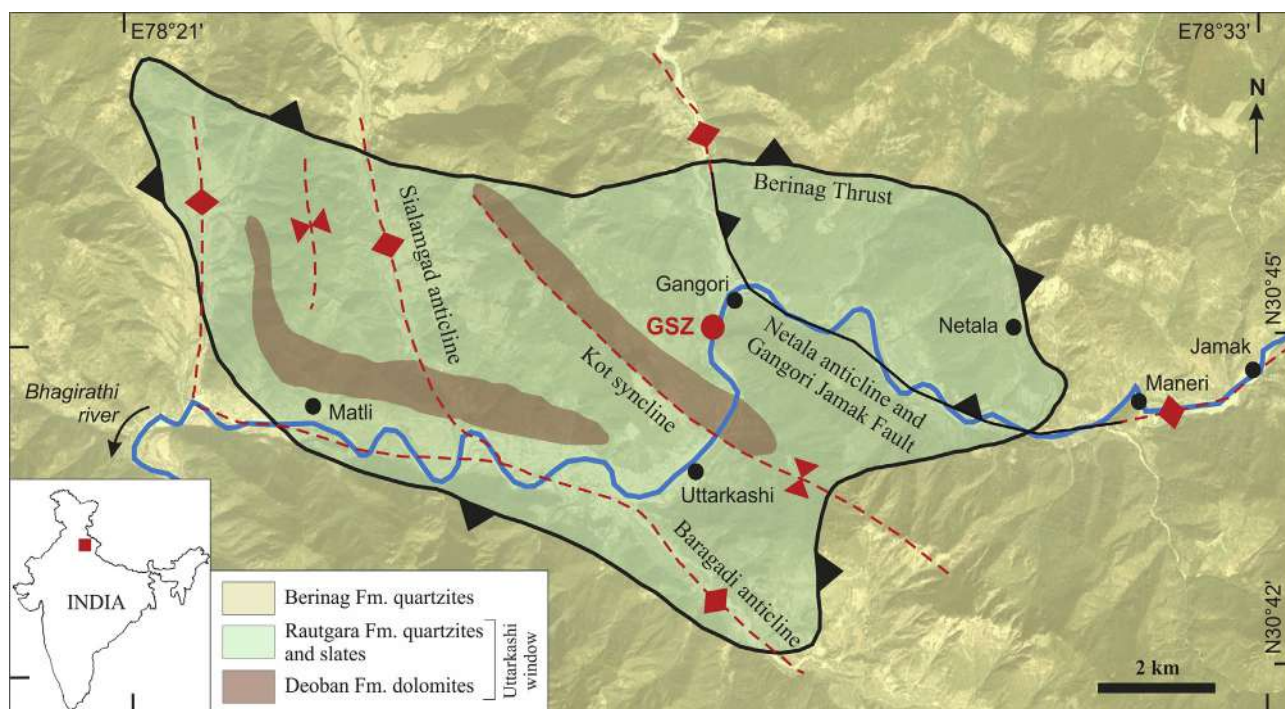


Fig. 1. Geological map compiled from Jain (1971), Agarwal and Kumar (1973), Valdiya (1980) and superposed on the Google Earth satellite imagery. Red filled square in the inset and the circle in the main figure indicate the study area: the Gangori Shear Zone (GSZ). Note near the location Maneri, unusual turn of the river is due to a dam constructed there. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

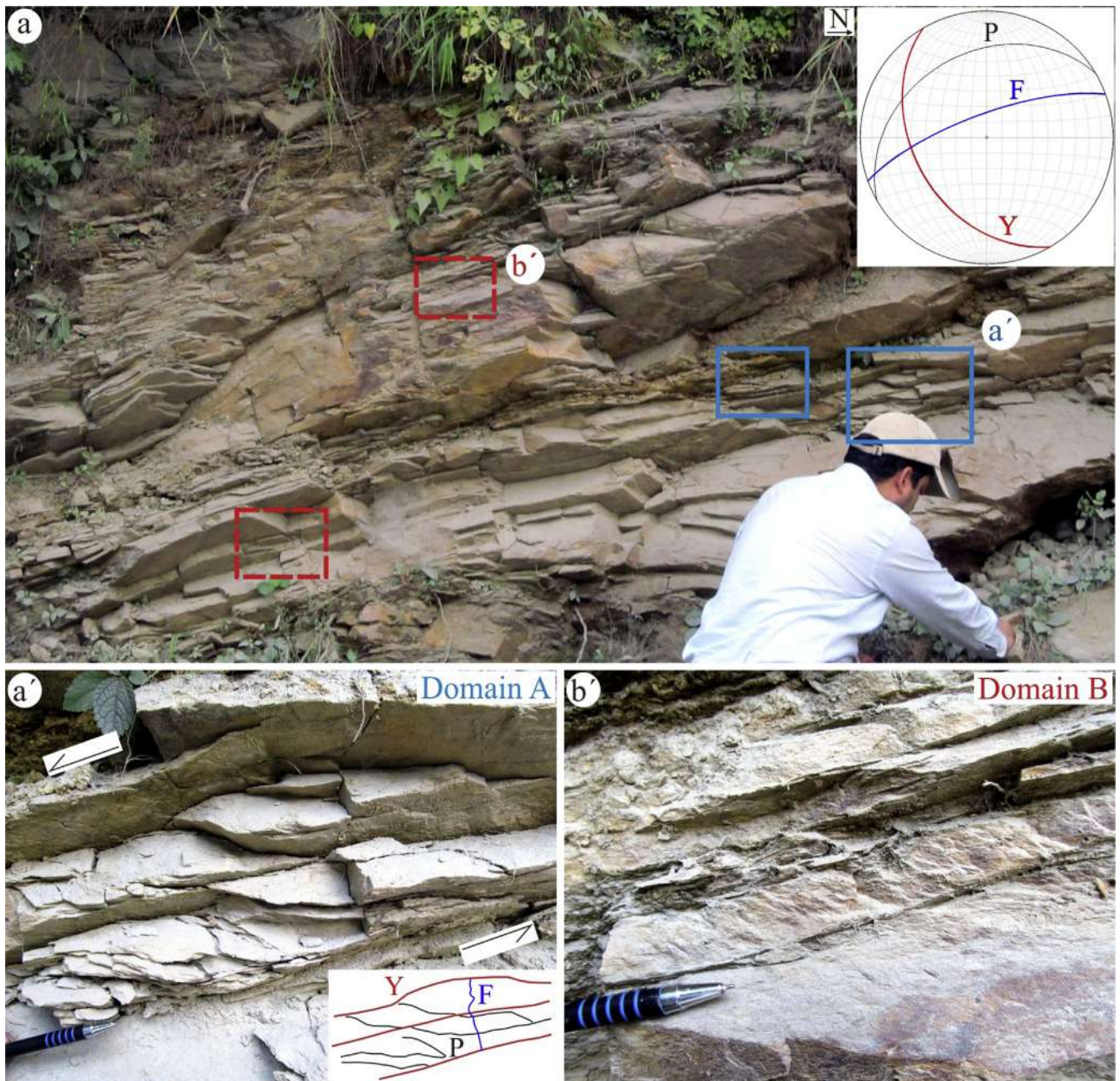


Fig. 2. Field observations. (a) Exposure at Gangori Shear Zone (GSZ). S. Mukherjee (~80 cm inside snap) as marker. Rectangles show the parts from where samples were collected. Blue solid rectangles: 'domain-A'; red-broken rectangles: 'domain-B'. Streplot in the inset: Y-plane: $150^{\circ}/42^{\circ} \rightarrow 240^{\circ}$, P-plane: $60^{\circ}/35^{\circ} \rightarrow 330^{\circ}$, fracture plane: $70^{\circ}/75^{\circ} \rightarrow 340^{\circ}$. (a') Domain-A: P-planes developed. ~6 cm of pen is visible, as marker. (b') Domain-B: P-planes not developed. ~5 cm of pen is visible, as marker. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

of clinocllore and illite (Supplementary Fig. 1), which are common clay minerals in shear zones (e.g., Lacroix et al., 2012; Buatier et al., 2013). The glycolated study confirmed the absence of clays of expanding phases.

3.3. Microstructures

XZ-sections (perpendicular to the trend of Y-plane and parallel to the dip direction) of the oriented samples were used for microstructural investigation. Narrow range of grain size variations, curved shear planes, marginal recrystallization of quartz grains etc. indicate intense shearing in domain-A (Fig. 3a1, a2, a3). On the other hand, in domain-B coarser framework grains with symmetric- and asymmetric mantled porphyroclasts (Fig. 3b1, b2, b3) indicate broader grain-size

distribution (quantification in Section-5). Although, the outcrop of domain-B is devoid of P-planes, evidences of intense ductile shear, deciphered from mantled porphyroclasts (Fig. 3b2, b3) and a few S-C fabrics (Fig. 3b1), were observed under an optical microscope. The micro-fractures present in the two domains are also dissimilar. The inter-granular extension fractures in domain A are mainly filled with clays and cross-cut the pre-existing ductily deformed veins and crenulations (Fig. 4). Whereas, in domain B, the less abundant inter-granular fractures are quartz-filled, with local drag along them (Fig. 5a, c). Moreover, grain-size reduction by intra-granular fracturing is more pronounced in domain B (Fig. 5a, b, d).

Domains A and B show various grain boundary mobility features (Stipp et al., 2002; Passchier and Trouw, 2005), such as: cataclastic flow ($< 300^{\circ}\text{C}$) is indicated by inter-granular fractures (Fig. 4) and

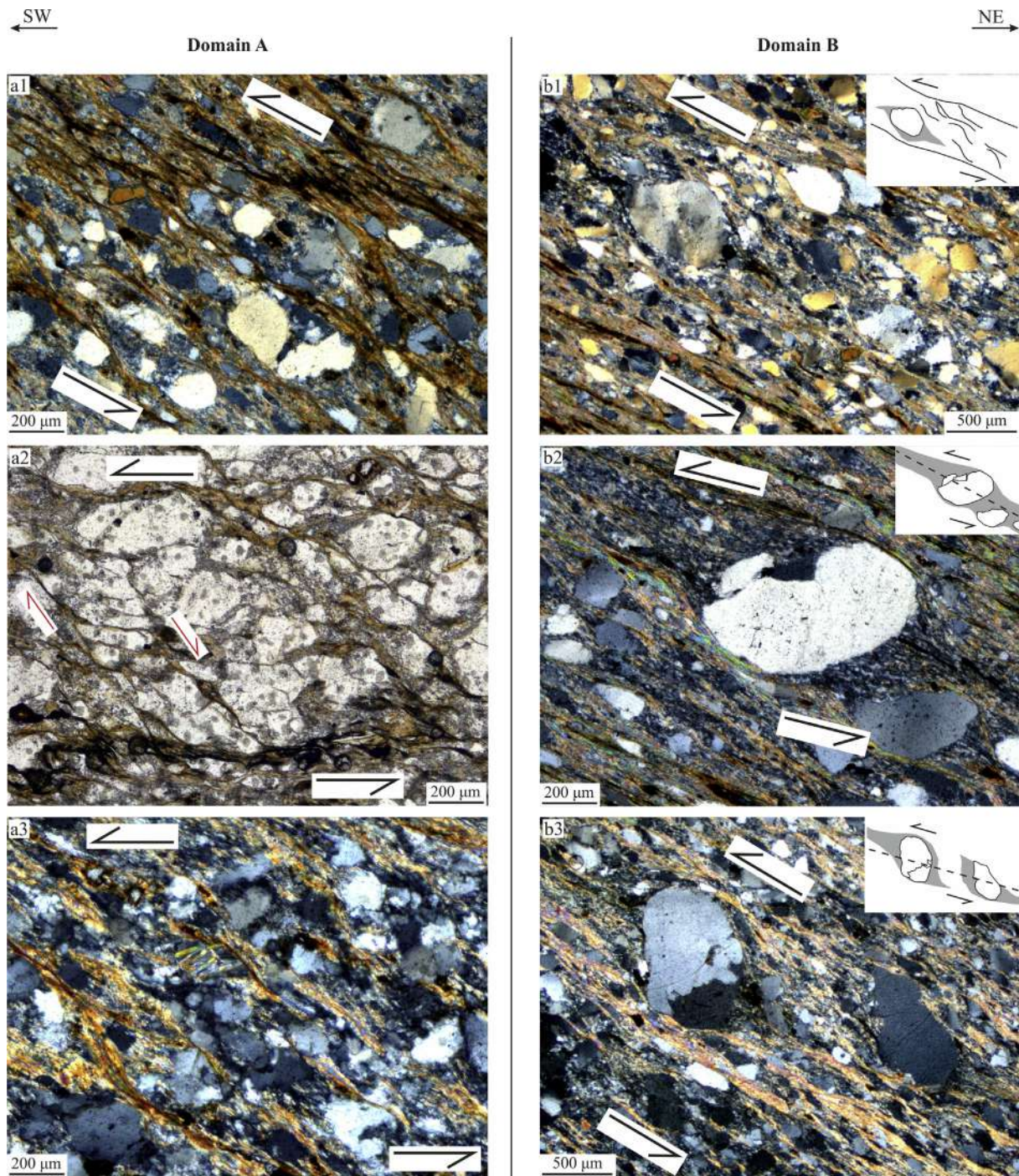


Fig. 3. Comparison of microstructures in domains A and B. Sub-figures a1, a2, a3 are from domain A, and b1, b2, b3 are from domain B. In all the figures NE is to the right. **(a1)** Quartz porphyroclasts embedded in finer matrix. The shear planes are present in the matrix and don't cross cut the quartz grains. The marginal recrystallisation of the quartz grains and the presence of clays along the shear planes are to be noted. Cross polarized light. **(a2)** Alignment of clays and mica represent the overall shear pattern of the rock. Red half arrows: antithetic shear. A coarse quartz grain fragmented into several sigmoid grains. Plane polarized light. **(a3)** Undulose extinction and marginal recrystallization of quartz. Cross polarized light. **(b1)** Strong mylonitic foliations, curved shear planes in the quartz rich part, neocrystallisation at the grain boundaries, undulose extinctions are to be noted. Cross polarized light. **(b2)** Symmetric pressure shadows (review in Mukherjee, 2017) formed at two sides of a quartz grain. Cross polarized light. **(b3)** σ -shaped tails near quartz clasts document shearing (black half arrows). Intra-granular healed fracture and the sutured sub-grain boundary in the central grain are to be noted. Cross polarized light. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

fragmentation of grains (Fig. 5). Alignment of fluid/solid inclusions along healed micro-cracks (Fig. 3a2, b2), which can be called a kind of “Tuttle lamellae” (review in Anders et al., 2014), also signifies the same. Symmetric- (Fig. 3b2) and asymmetric mantled porphyroclasts (Fig. 3b3) connote pressure solution and re-deposition of materials.

Whereas, bulging in grain boundary (Fig. 3a1), neo-crystallization along grain boundaries (Fig. 3a3, b1) indicate bulging recrystallization (300–400 °C).

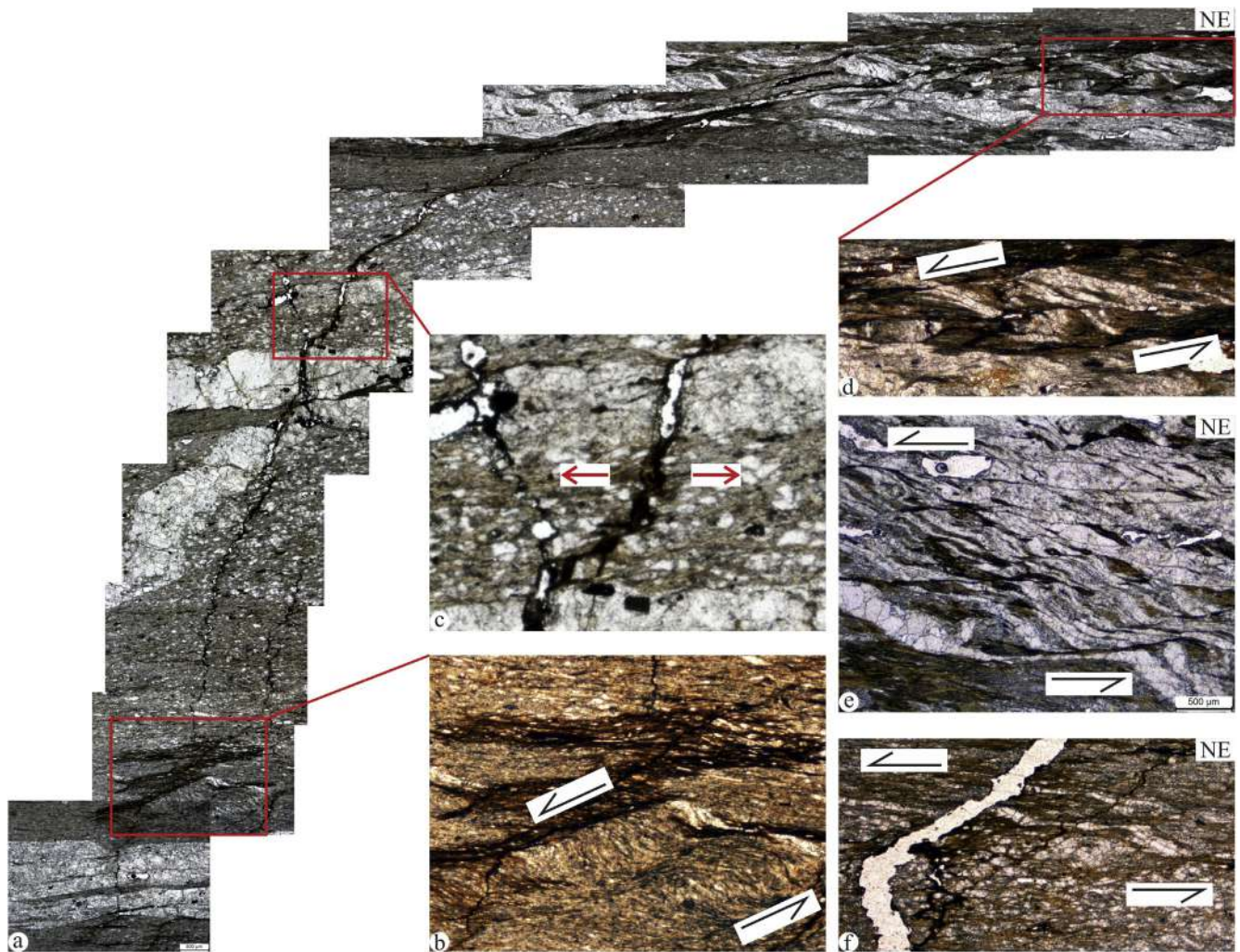


Fig. 4. Extensional-/dilatant shear fracture noted in XZ-section of domain-A. All figures in plane polarized light. (a) Mosaic showing the overall appearance of the fracture. In the central and lower part of the mosaic, where the quartz porphyroclasts are more abundant, the fracture is present at high-angle displaying shear-sense. Towards the upper part of the mosaic, where fine grained matrix and sheared quartz veins are present, the fracture gradually becomes parallel to the shear P. Width of each of the images is ~ 3.5 mm. (b) Shear fabric (shear sense: black half arrows) in finer matrix. Younger extensional fracture as in mosaic 'a' cuts it across. (c) Note the wide opening (probable extension direction: red half arrows) and stepping of the fracture. (d) Top-to \sim SW fore-sheared (black half arrows) quartz veins cross-cut by younger fractures. (e) Observations resembling 'd' made from another part of the thin-section. (f) Fore-sheared (black half arrows) quartz veins cross-cut by younger extensional fractures. Both the features were generated by the same shear sense. Width of image ~ 3.5 mm. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

3.4. Rheological issues

The studied rock samples show evidences of intense ductile deformation, viz. sheared veins and foliations, pressure shadows, S-C fabrics etc. The rheology of a sheared rock-whether Newtonian or not-may be inferred from microstructures. For example, mantled porphyroclasts can show eye-shaped separatrix, absence of stair stepping in wings for Newtonian flow (review in Mukherjee, 2017) and bow-tie shaped separatrix, stair stepped wings for the non-Newtonian pattern (Passchier and Sokoutis, 1993; Passchier, 1994). However, the type of separatrix also depends on various other factors, viz., the aspect ratio of the porphyroclast, ratio of pure shear to simple shear etc. (Pennacchioni et al., 2000; Mandal et al., 2001).

Ductile deformation of rocks following Newtonian viscous behaviour is characterized by grain boundary sliding by diffusion mass transfer and grain boundary dislocation mechanisms. Ductile deformation of rocks following Non-Newtonian behavior reflect dominantly crystal slip plasticity by recovery processes, including dislocation climb and pile-up, sub-grain rotation and marginal recrystallization (Dimanov et al., 2015). Marginal recrystallisation was

observed from both the samples (Fig. 3). Also, stepped (sigma-structure in Fig. 3b3) as well as non-stepped (symmetric clasts in Fig. 3b2) tails are associated with the porphyroclasts. This indicates roughly a Newtonian rheology for the samples from domains A and B.

Evidences of brittle deformation, e.g., presence of meso-scale Y-and P-planes and inter-/intra-granular micro-fractures, have also been noted in the samples from both the domains (Figs. 4 and 5). Brittle deformation is more preferred in the upper crustal rocks, whose rheological behavior can be approximated convincingly as linear elastic (Pollard and Fletcher, 2005; Turcotte and Schubert, 2014). Fracture mechanics presumes linear elastic behavior of rocks to investigate fracture propagation, the stress distribution at fracture tips, and cause of different fracture patterns (Irwin, 1960; Mandl, 2005; Stoeckhert et al., 2015). But, Gudmundsson (2011) argues that such an assumption is valid for $< 1\%$ of strain. Karato (2008), however, categorized both brittle- and plastic deformations under non-elastic deformation.

On the other hand, considering the co-existence of both ductile and brittle features, a visco-elastic rheology can be assigned for these rocks. Visco-elastic material, behaves as an elastic solid for short time-scales, but on geologic time scales (10^4 yr) it acts a viscous fluid (Turcotte and

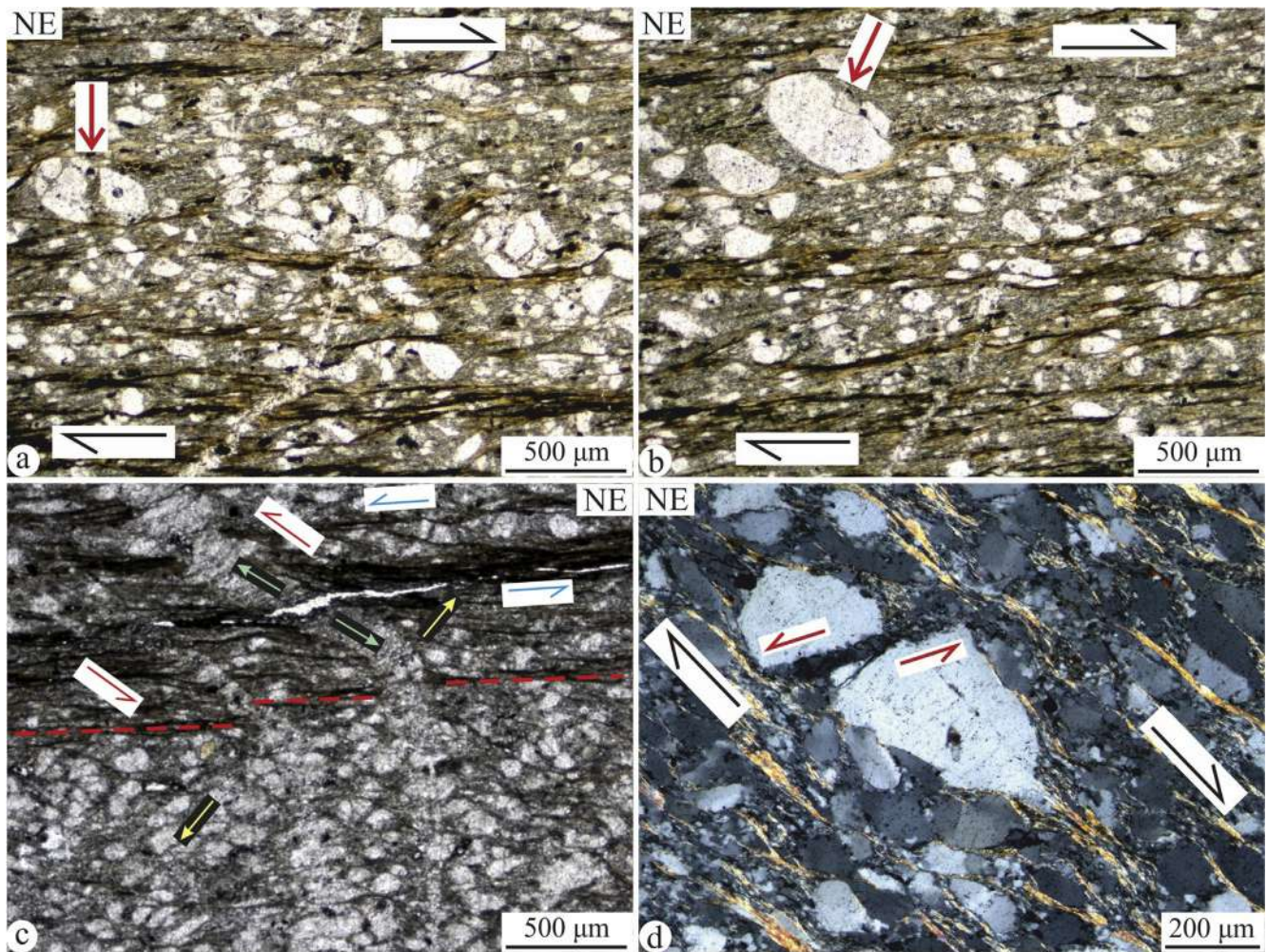


Fig. 5. Compressional and extensional features in XZ-section of domain-B. Black half-headers indicate overall shear sense. (a, b) Clays and flaky minerals define the Y- and P- planes, which indicate compressional fore shear. The pull-apart (Hippert, 1993; Mukherjee, 2010) features (red full arrow) indicate extension. (c) The vein is sheared with a minor drag along them (red half-headers). This shear sense matches with the top-to-SW sense as seen in the whole rock (blue half-headers). The extension direction for the sheared quartz vein (yellow arrows) is at a high-angle with a younger tensile crack that crosscuts it (green full arrows). Plane polarized light for a, b, c. (d) Antithetic brittle extensional sheared (red half-headers) quartz porphyroclast in a foreshear (black half-headers) regime. Cross polarized light. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

Schubert, 2014; Fossen, 2016). Such materials are more suitable to model the lower crust deformations. In the present context, both the viscous and the elastic features might be correlated with the active aseismic-seismic cycles going on in this region of high seismicity (Rajendran et al., 2017 and references therein).

4. Finite strain analysis and vorticity measurement

4.1. Strain markers

Elliptical quartz grains are widely used strain marker as they record the deformation process through the change in shape (e.g., Xypolias and Koukouvelas, 2001). The plastically deformed quartz grains are selected for the R_f - ϕ analyses. Whereas, for vorticity analysis, rigid quartz grains with pressure shadows (from domain B) were used. Strain analyses involve several assumptions (Xypolias, 2010 and references therein; Sengupta and Chatterjee, 2015). We discuss them below taking examples from our samples.

1. The studied rock samples show Newtonian rheology (Section-3.4), which is a prerequisite for the strain and vorticity analyses.
2. Recrystallized and fractured grains should not be analyzed since

their strained shapes get modified by those processes. Clasts should be freely-rotating rigid ellipsoids, perfectly bonded to the matrix and ought not mutually interact mechanically. Strain partitioning at the clast interface should be avoided. In GSZ thin sections, both elliptical and non-elliptical types of clasts exist within a fine-grained matrix (Fig. 3), which validates the rationale for strain analyses. Grains that are either fractured or are in mutual contact were avoided, and semi-elliptical/irregular shaped isolated unfractured grains were selected in this study.

3. The thin-section should be orthogonal to the rotation axis of the porphyroclasts, otherwise the methods will underestimate the mean kinematic vorticity number (W_m). This also happens when the sample lacks grains with large aspect ratios (R_f). W_m is overestimated if the clasts did not attain a stable position. Well-developed δ -type clasts or plots with sharp cut-off points (in the R_f - ϕ diagram) signify that the strain was sufficient enough for the grains to stabilize. Following these cautions, The XZ-sections (perpendicular to the strike of the Y-plane) from both the domains were used in the present study. In our study, the chosen clasts have overall a wide range of aspect ratios: 1.00–4.65 in domain-A, and 1.02–5.94 in domain-B.

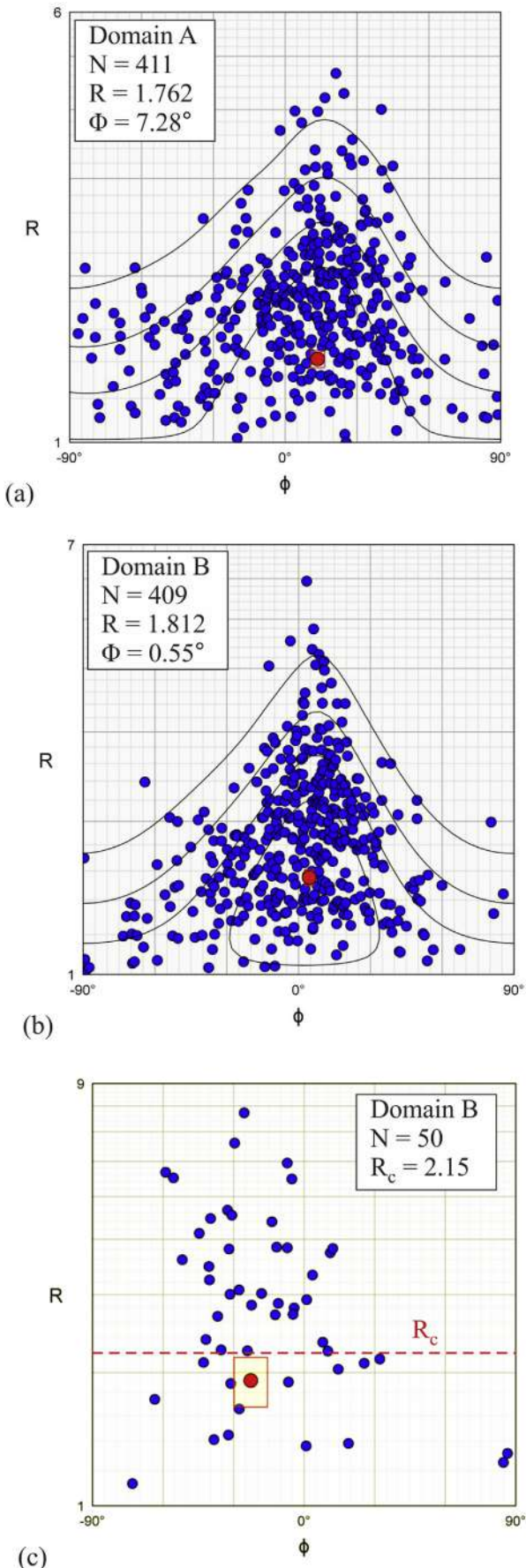


Fig. 6. Strain analyses and KVN measurements. Red dot: Mean values of R (i.e., R_f) and ϕ . (a, b) R_f - ϕ analyses results for domains A and B, respectively. (c) Kinematic vorticity number calculation by PAR method for domain B. Red broken line indicates the cut-off point and R_c is the corresponding R value. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

4.2. Method

The R_f - ϕ method (Dunnet, 1969; Lisle, 1985) is commonly used to analyze strain. R_f is the ratio of the lengths of major-to minor axes of the ellipse, and ϕ is the angle between the major axis of the ellipse and a reference direction, which is usually the primary shear direction. The R_f - ϕ values were obtained for ~ 410 grains from each of the thin-sections prepared. From these values, the R_f - ϕ graphs were plotted and the vector mean of ϕ and the harmonic mean of R_f were calculated.

The Kinematic Vorticity Number (KVN; Hanmer and Passchier, 1991; review in Xypolias, 2010) indicates coaxiality of the successive deformation stages and quantifies the % of pure- and simple-shears. Amongst the various approaches, the Porphyroclast Aspect Ratio (PAR; Passchier, 1987) method uses strained elliptical clasts to measure the KVN. A critical value of R (R_c) is marked on the R_f - ϕ graph (e.g., Fig. 8c of Xypolias, 2010) to mark the cut-off point. From the R_c value, the mean KVN (W_m) is calculated (eqn. (1)).

$$W_m = (R_c^2 - 1)/(R_c^2 + 1) \quad (1)$$

4.3. Results

The EllipseFit v3.3.0.62 software was used to generate the ' R_f - ϕ ' diagrams. R_f values of 1.762 and 1.812 were obtained from domains-A (Fig. 6a) and -B (Fig. 6b), respectively. The calculated KVN for domain B is 0.65 (Fig. 6c), indicating $\sim 55\%$ pure shear. Such a combination of pure- and simple-shear is common in natural shear zones (e.g., Fossen and Cavalcante, 2017; Long et al., 2017) and indicates that the rock would eventually fail by dilatant shear fractures/hybrid fractures (Ramsey and Chester, 2004; Ishii, 2015).

5. Grain size analyses

Areas of 410 quartz porphyroclasts from both the domains- A and B were measured (Fig. 7) using the software JMicroVision v1.2.5. The grain size for domain A is $< 40,000 \mu\text{m}^2$. Whereas, significant amount of coarser grains ($> 45,000 \mu\text{m}^2$) are present in the domain-B. Whether this is the major guiding criterion behind the selective formation of sigmoid brittle-shear planes (P-planes) in domain-B, is addressed in the following numerical modeling.

6. Numerical modeling

6.1. Theory & background

Brittle fracturing of rocks, the associated stress-strain distribution as well as the factors responsible for their initiation and propagation, have been widely studied with the help of numerical simulations (e.g., Camacho and Ortiz, 1996; Hoek and Martin, 2014 and references therein; Zhang and Zhao, 2014; Gao et al., 2016; Hattori et al., 2017; Wu et al., 2017). Although, most of the previous studies considered elastic-plastic, visco-elastic or visco-plastic rheological models to investigate brittle deformations (e.g., Sandiford et al., 2006; Behn et al., 2007; Kaus, 2010; Roland et al., 2010; Currenti and Williams, 2014; Ding and Lin, 2016; Thompson and Parsons, 2016), purely elastic rheological model was preferred by many as well (e.g., Burchardt, 2008; Xu et al., 2012; Lu et al., 2014; Guallini et al., 2015; Wei et al., 2015; Nabavi et al., 2017).

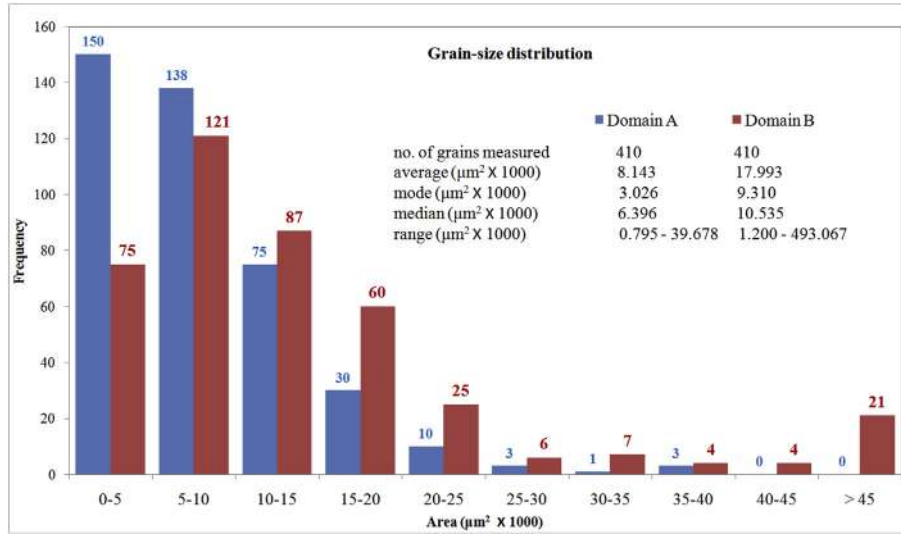


Fig. 7. Grain-size distribution from domains -A and -B. Grain sizes were measured using JMicroVision software (v 1.2.5).

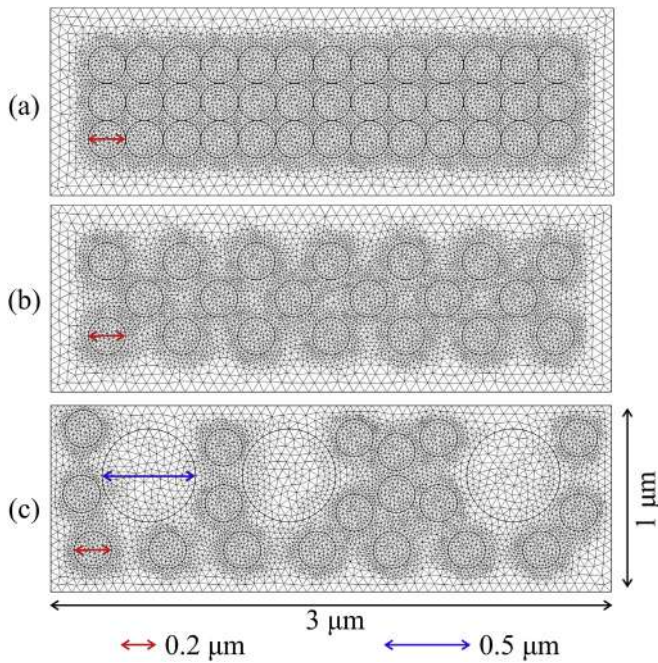


Fig. 8. Geometry of the model domains and the meshing. (a) Model-1, (b) Model-2 and (c) Model-3.

This study represents an approximation to the more realistic non-linear deformation processes of the upper crust. Hence, an isotropic, linear elastic behavior was chosen for the materials incorporated in our models. Brittle deformation of rocks can be studied with the help of either the Drucker-Prager or the Mohr-Coulomb failure criterion (Hobbs and Ord, 2015). The former is often approximated as a ‘smoothed

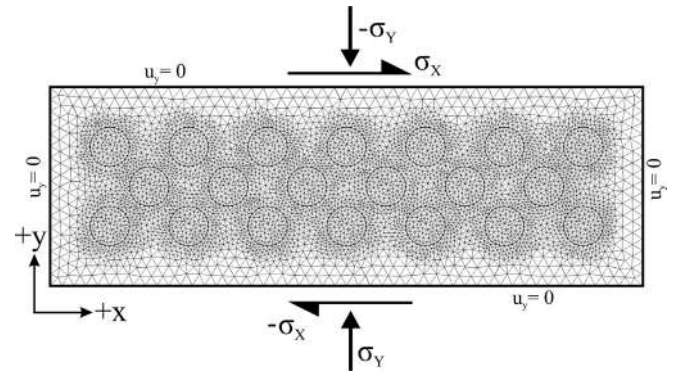


Fig. 9. Stresses applied on the upper and lower boundaries of the model domain. Negative sign implies that the stress is directed towards the negative side of the X- or the Y-axes.

version’ of the latter in a 3D scenario/model (Tetreault and Buitier, 2012; Currenti and Williams, 2014; Cervera et al., 2016; Carcione et al., 2018).

6.2. Governing equations

Equations (2)–(4) must be solved to determine the state of stress and displacements at the end of a 2D quasi-static deformation of an isotropic and linear elastic material.

$$\sigma_{ij} = \lambda \delta_{ij} \sum_k \epsilon_{kk} + 2\mu \epsilon_{ij} \quad \text{Hooke's law} \quad (2)$$

$$\nabla \cdot \sigma + F = 0 \quad \text{static equilibrium} \quad (3)$$

$$\epsilon = \frac{1}{2} [\nabla u + (\nabla u)^T] \quad (4)$$

Table 1

Physical parameters of the materials used.

Material	Density (kg m ⁻³)	Young's Modulus (GPa)	Poisson's Ratio (unitless)	Cohesion/Inherent shear strength (MPa)	Angle of Internal friction (radian)
Sandstone	2000–2800 ^[1,2]	10–60 ^[1,2]	0.1–0.3 ^[1,2]	25.5–27.2 ^[3,4]	0.46–0.6 ^[1,5]
Quartzite	2500–2700 ^[1,2]	40–60 ^[1]	0.15–0.20 ^[1]	70.6 ^[4,6]	0.45–1.05 ^[1,5]

References: 1. Gudmundsson (2011), 2. Henderson and Henderson (2009), 3. Zhang et al. (2008), 4. Goodman (1980), 5. Pollard and Fletcher (2005), 6. Takahashi and Tanaka (2017). Note: the mean values of the ranges are used in our models, except for the cohesion for quartzite where a single value is obtained from the literature.

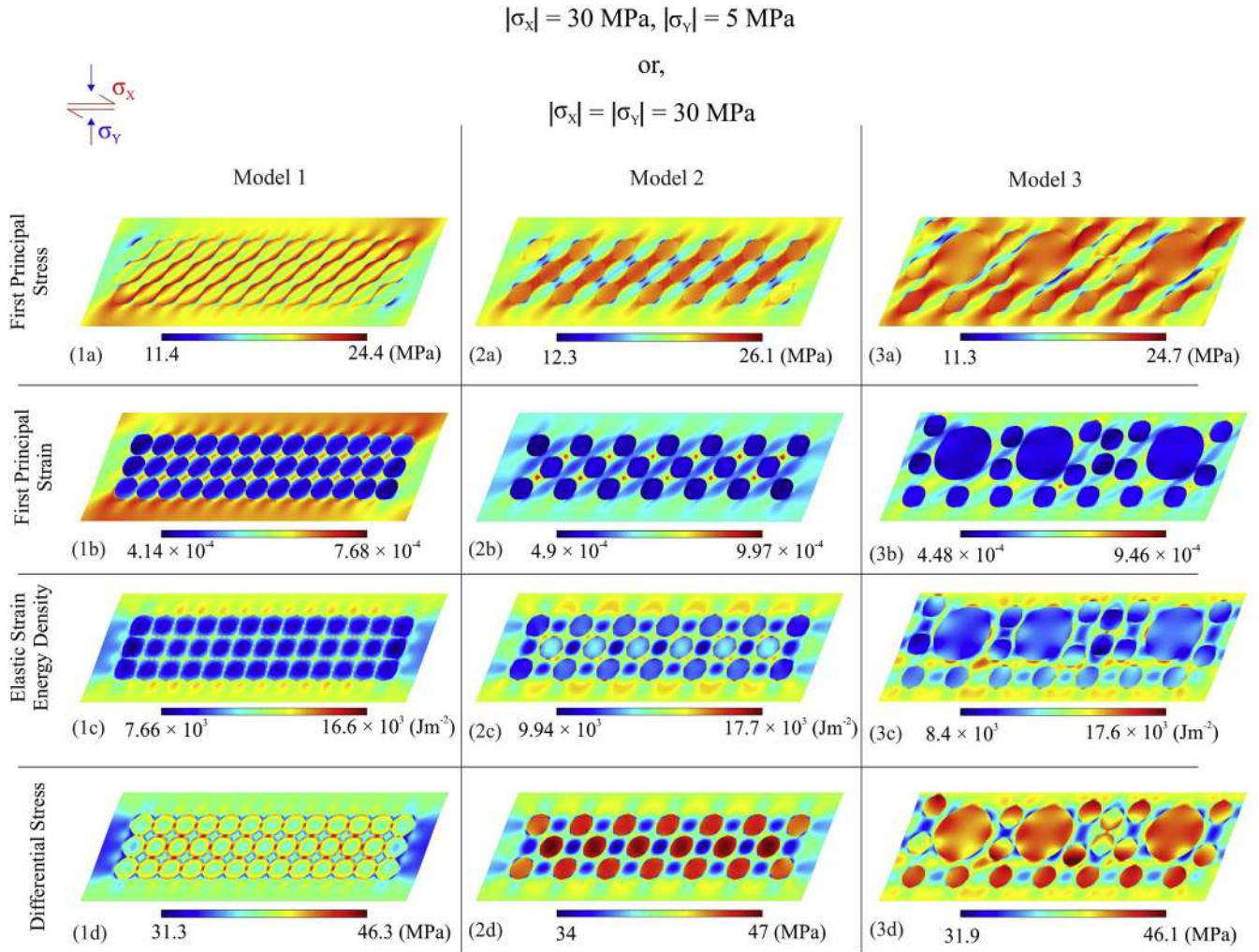


Fig. 10. Variations in the response of the three models to general shear, where $|\sigma_x| > |\sigma_y|$ or, $|\sigma_x| = |\sigma_y|$. Joule meter⁻² is the unit of surface tension or stiffness.

where, σ (stress matrix) = $\begin{bmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & \sigma_{yy} \end{bmatrix}$; ϵ (strain matrix) = $\begin{bmatrix} \epsilon_{xx} & \epsilon_{xy} \\ \epsilon_{yx} & \epsilon_{yy} \end{bmatrix}$ = $\begin{bmatrix} \frac{\partial u}{\partial x} & \frac{1}{2} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \\ \frac{1}{2} \left(\frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right) & \frac{\partial v}{\partial y} \end{bmatrix}$; ∇u (displacement gradient) = $\begin{bmatrix} \frac{\partial u}{\partial x} & \frac{\partial u}{\partial y} \\ \frac{\partial v}{\partial x} & \frac{\partial v}{\partial y} \end{bmatrix}$; λ

and μ are Lamé constants; and δ_{ij} (Kronecker delta) = $\begin{cases} 1, & \text{if } i = j \\ 0, & \text{if } i \neq j \end{cases}$; F is the body force (Bahat et al., 2005; Jaeger et al., 2009; Karato, 2008; Gerya, 2010; Newman, 2012; Perez, 2017).

The effect of intermediate principal stress (σ_2) on brittle failure is only considered by the latter (Jaeger et al., 2009). Colmenares and Zoback (2002) showed that failure criteria such as Mohr-Coulomb or Hoek-Brown, which ignores the influence of σ_2 , can be used. Shear failures, the focus of this study, are best anticipated by the Mohr-Coulomb criterion (eqn. (5); Paterson and Wong, 2005; Bai and Wierzbicki, 2010; Cox, 2010; Kaiser and Kim, 2015):

$$\sigma_1 \{ \sqrt{(1 + \mu_i^2)} + \mu_i \} - \sigma_3 \{ \sqrt{(1 + \mu_i^2)} - \mu_i \} - 2S = 0 \quad (5)$$

where, σ_1 : maximum principal stress; σ_3 : minimum principal stress; μ_i : coefficient of internal friction and S : inherent shear strength or cohesion (Pollard and Fletcher, 2005; Jaeger et al., 2009). Being representative of the Lesser Himalayan section, the GSZ is a part of the India-Eurasia collisional-compressional domain (e.g., Mukherjee et al., 2015). Hence, the X-axis and the σ_1 orient NE-SW, the Y-axis and the σ_3

is vertical, and the σ_2 is orogen parallel, i.e., NW-SE.

Eqn. (5) was used to determine the locations susceptible to shear fracture. With the help of finite element numerical simulations, the values of the expression on the left hand side of eqn. (5) (Yield Function: Y_F) was determined throughout the model domain. Cohesion (S) in eqn. (6) is also related to the uniaxial compressive strength (C_U) and coefficient of internal friction (μ_i) of the material (Pollard and Fletcher, 2005):

$$S = \frac{C_U}{2\{(\sqrt{(1 + \mu_i^2)} + \mu_i)\}} \quad (6)$$

Previous authors have often incorporated a combination of Mohr-Coulomb and tensile failure criteria to model/study brittle deformation (Wilson et al., 2007; Lunn et al., 2008). As per Zhu and Tang (2002) and Jaeger et al. (2009), macroscopic shear failures often involve tensile damage at smaller scales. However, in our model such a combination was neglected for simplification purposes, and hence tension cut-off has not been included.

6.3. Model setup

We ran three 2D models: 1, 2, and 3 (Fig. 8). Each of them consists of circular quartz grains within a rectangular ($1 \mu\text{m} \times 3 \mu\text{m}$) sandstone matrix (rheological parameters in Table 1). In model 1 (Fig. 8a), the sizes of all the quartz grains are identical: $0.2 \mu\text{m}$ diameter. They are

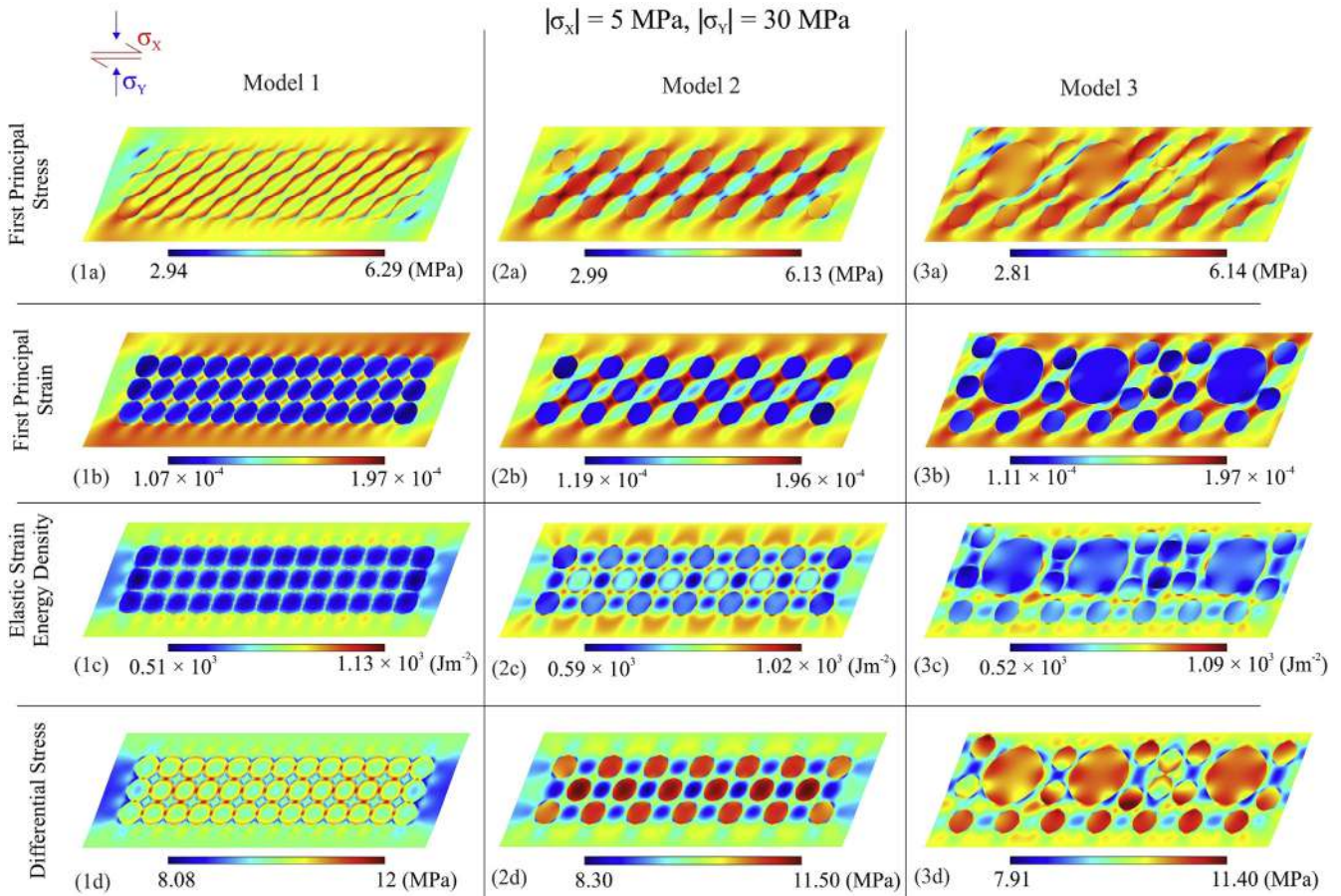


Fig. 11. Variations in the response of the three models to general shear, where $|\sigma_x| < |\sigma_y|$.

densely packed with mutual point contact. In Model 2 (Fig. 8b), the grain size is same as in model 1, however, unlike model 1, the grains are not in contact with their neighbours. The closest distance between two adjacent grains is $\sim 0.28 \mu\text{m}$. Model 3 (Fig. 8c) contains grains of two different sizes. Larger grains have a diameter of $0.5 \mu\text{m}$. The size of the smaller grains is same in model 1 and 2. But, the largest distance between the two neighbouring small grains is $0.4 \mu\text{m}$ in model 3. As in model 2, none of the grains of model 3 are in mutual contact. Models 1, 2 represent domain A, and Model 3 domain B.

In our numerical analyses, eqns. (2–4) were solved using the finite element method (Courant, 1943; McHenry, 1943; Zienkiewicz and Taylor, 2000) in COMSOL Multiphysics v5.0 software. As in most of continuum numerical models, the materials in this study were considered to be (nearly) incompressible (Buitter, 2012). Dilation due to shear was not considered. For quasi-static set up, the imposed acceleration as well as the kinetic energy of the system (both generated due to application of stress) were neglected (Buitter, 2012; Hobbs and Ord, 2015). Now given that this is a time-independent study, results are independent of the inertial parameters. We chose triangular mesh in 2D finite element (FE) models, as practiced widely (Pepper and Heinrich, 2006; Frey and George, 2008; Ismail-Zadeh and Tackley, 2010; Tadmor et al., 2012; Fenner, 2013). COMSOL consists of automatic mesh generation module, which discretizes both the matrix and clast domains into triangular elements, with advancing front tessellation (Zhang, 2016 and references therein). The element concentration is higher at the clast boundaries since the sizes of meshes reduce close to the curved boundaries.

The coordinate axes X and Y are as per Fig. 9. Assuming a plane strain, all the models were subjected to general shear. σ_x denotes the shear stress parallel to the X-axis on the two length boundaries of the

rectangle, and towards opposite directions. Compressive stress σ_y apply parallel to the Y-axis on the same boundaries. The velocity components along the Y-direction (u_y) were restricted to zero (no velocity boundary condition) for all the four edges of the rectangle, in order to inhibit rotation of the geometry during deformation (Johnson et al., 2009; Nabavi et al., 2017 and references therein). For the sake of simplicity, the effects of grain size reduction with deformation were avoided. Our models also presume that, unlike the natural case referred by Warren and Hirth (2006), no strain partitioning took place.

We ran two different experiments on models 1–3. In the first experiment (Experiment 1) models 1, 2 and 3 were subject to three different stress conditions: *i.* The layer parallel shear stress (σ_x) = 30 MPa, the layer normal stress (σ_y) = 5 MPa; *ii.* $\sigma_x = \sigma_y = 30$ MPa; *iii.* $\sigma_x = 5$ MPa, $\sigma_y = 30$ MPa. The aim of Experiment 1 is to check the effects of variable grain sizes on various parameters, such as First Principal Stress, First Principal Strain, Elastic Strain Energy Density (ESED) and the Differential Stress. In another experiment (Experiment 2), identical stresses were applied to the three models with $|\sigma_x| = 390$ MPa and $|\sigma_y| = 120$ MPa. Experiment 2 was conducted to understand the effect of variable grain size and distribution on the spatial distribution of the brittle shear planes/fractures, P-plane in particular. We also test the dependency of the failure pattern on grain-size variation and distribution.

6.4. Results and interpretations

6.4.1. Experiment 1

The behavior of the models under different σ_x and σ_y conditions have been presented in Figs. 10 and 11. For $\sigma_x = \sigma_y$ and $\sigma_x > \sigma_y$, the models 1–3 generated identical results. The results show that, larger the

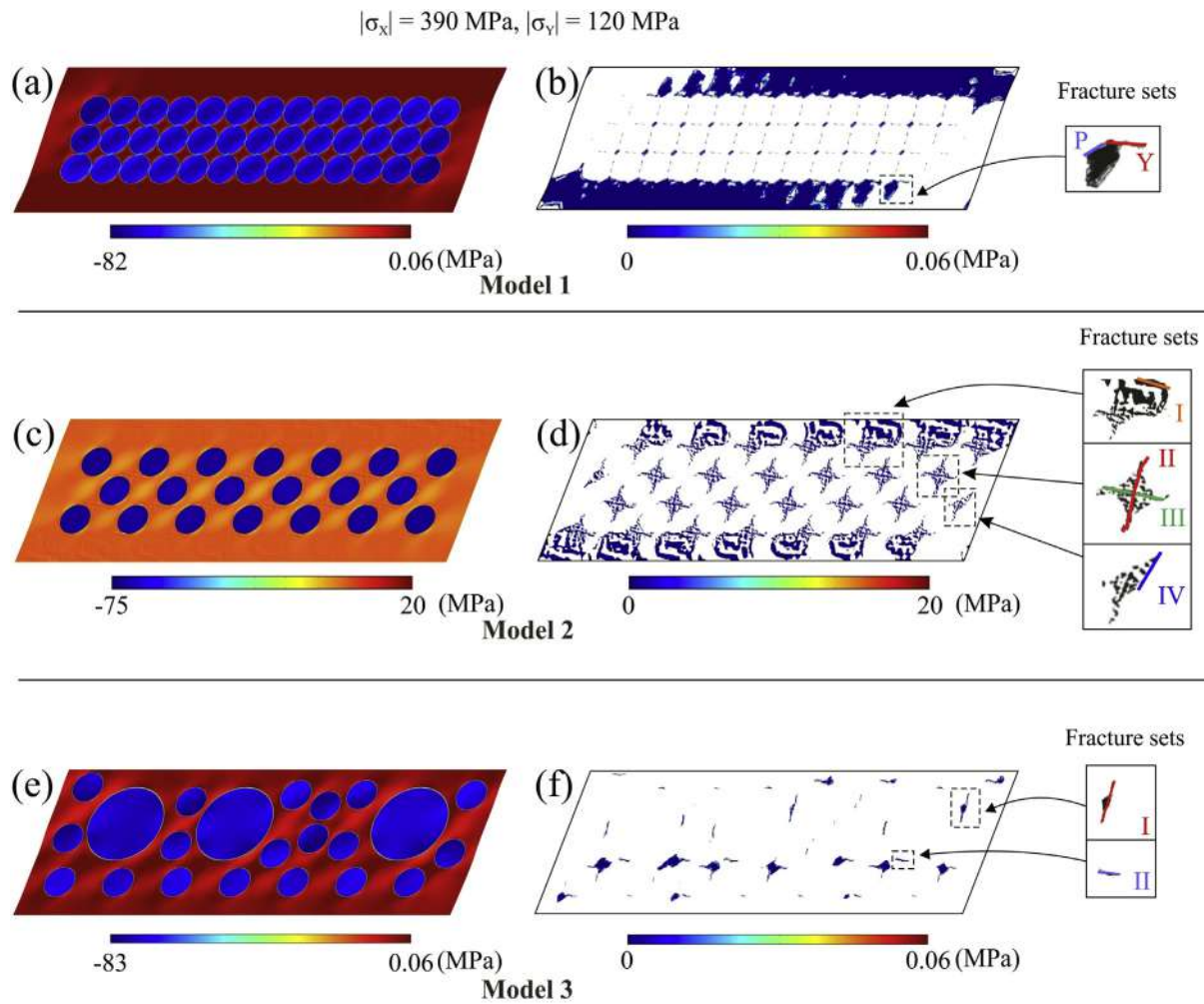


Fig. 12. Values of the yield function (Y_F ; right hand side expression in eqn. 5) throughout the domains after deformation. $|\sigma_x|$ & $|\sigma_y|$: magnitude of force per unit length applied on the upper and lower boundaries of the rectangular domain, parallel to X- and Y-axis respectively. (a, c, e) show total range of yield function (Y_F) throughout the model domains. The images of the right column (b, d, f) show only those zones where the values of the $Y_F \geq 0$. The inset diagrams represent the zoomed version of the corresponding sub-domains. The types of fractures have also been marked.

grain-size, lower the overall rock ESED. The ESED and differential stress is lowest in Model 1, where the quartz grains are in contact. The grains in contact behave as a larger grain of cumulative size. Models 2 and 3 show that the presence of quartz grains decreases the ESED of the intergranular spaces.

6.4.2. Experiment 2

Shear fractures are more likely to develop at places with $Y_F \geq 0$ (Pollard and Fletcher, 2005; Gudmundsson, 2011). Value of Y_F varies from -83 MPa to 20 MPa in our models (negative symbol indicates absence of shear fracture). The solutions obtained, show that in case of Model-1, the curved shear-fractures are mostly restricted outside the area occupied by clasts. In other words, they do not pass through/cut across the grains. This is also seen in the domain A microstructures (Fig. 3a1). Also, the acute angle between the fractures and the possible Y-shears, increase from $\sim 32^\circ$ close to the clasts to $\sim 61^\circ$ near the boundary of the model domain (Fig. 12a). The ones at $< 45^\circ$ to the horizontal (Y-shear) are possibly the P-planes (Meyer et al., 2017). On the other hand, for Model-2, four sets of shear fractures develop (Fig. 12b). Close to the domain-boundary, the Set-I fractures form at $\sim 40^\circ$ with the horizontal (domain boundary). Whereas in between the grains fractures are restricted to somewhat rhombic domains, whose diagonals define another two sets of fractures: one of which is at high angle (Set II $\sim 78^\circ$) and the other one being sub-parallel (Set III), to the

horizontal (Fig. 12c and d). Similar shear fractures are observed in Fig. 3. Also, near the two lateral domain-boundaries another set of fractures Set IV ($\sim 50^\circ$ to Y-plane), are produced (Fig. 12b). These shear fractures appear to be more straight than those in Model-1. Model-3, however, shows two sets of shear fractures. One set, possibly the R'shear plane form at $\sim 77^\circ$ to the Y-plane (domain boundary) and the other set at $\sim 48^\circ$. The second set is present in between the clasts or between the clasts and the domain-boundary. Whereas, the high-angle ones are restricted near the lateral boundaries (which were parallel to Y-axis before deformation) of the model (Fig. 12c). Domain-B does show under microscope two sets of shear fractures: one at a high-angle to the Y-plane (possibly the P-plane) and the other at a gentler angle (Fig. 5a).

7. Discussions

In the field, the two domains- A and B are merely about a meter away. Both the domains have same mineralogy and display similar strain. Hence the domains can be considered to have experienced the same deformation throughout the geological time. Under microscope, both the domains show prominent signatures of phyllonitisation (Figs. 3 and 5; Wenk and Pannetier, 1990; Goodwin and Wenk, 1995) such as: (i) close-spaced phyllosilicate-rich shear planes; (ii) fragmentation of coarser grains; and (iii) intense preferred orientation of mainly flaky

minerals, e.g., micas. Profound fluid activities and presence of clays discriminate phyllonites from mylonites and cataclasites (Mancktelow and Pennacchioni, 2004; Jefferies et al., 2006). However, the mylonitic foliations are better developed/preserved in domain B. At the same time, micro-fractures present in the domains are dissimilar. Clay-rich extension fractures persist in the domain-A. Sample from domain-B dominantly exhibit intra-granular fractures (red arrows in Fig. 5b and c). Inter-granular fractures, though present, are much less in number and filled with quartz. The key difference between the domains were pointed out by the grain-size analysis (section 5), which shows a broader range of grain-size distribution in domain-B. This broader grain-size distribution enhanced diffusion creep in domain-B, and more importantly suppressed the effects of dislocation creep (Montési and Hirth, 2003). The observed differences in the two domains, from the presence of P-planes in field exposure to the discussed micro-structures, can be explained in this way.

General shear with equal kinematic vorticity numbers deciphered from the two domains indicate that the studied rock exposure underwent similar proportion of pure- and simple shear (section 4). Therefore, the numerical models utilize stresses both perpendicular and parallel to the Y shear planes. The domains have almost identical mineralogy and strain pattern. But, domain-B has larger sizes of quartz porphyroclasts, which has significantly reduced the overall strain of the body (Figs. 10 and 11). Finite element modeling clearly reveals similar dependence of spatial distribution of shear fractures on grain-size variation. P-planes are more prominent in Models- 2 (equigranular, isolated; equivalent to domain-A) and 3 (coarser grains, isolated; equivalent to domain-B). Moreover, coarser grain-size results in two sets of shear fractures, one at a high-angle to the domain-boundary, and another much lower angle. Interestingly, the P-planes develop earlier than the Y-planes in all the models. Similar conclusions came from other terrains (Skempton, 1966; Bartlett et al., 1981; Kirkwood and Malo, 1993) in meso- and micro-scale, but modeling remained due. Unlike that in Models- 2 or 3, the P-shear fractures in Model 1 (equigranular, close packed; equivalent to domain-A) are curved. The elastic strain energy density of those models shows that the coarser part has less energy and prefers to remain less deformed than the finer part. Hence, the coarser part of the natural exposure (domain-B) seems less strained under similar condition.

8. Conclusions

Through this study, the effect of grain size on brittle failure has been examined in naturally deformed samples and the following observations have been made:

1. Two domains were demarcated in the field exposure based on the presence of brittle P-planes.
2. XRD analyses and thin-section observations indicate that rocks in the two chosen domains have same mineralogy. Therefore, development of P-planes preferentially in one of those domains cannot arise from mineralogical disparity. Strain analyses further shows that both the domains underwent similar general shear deformation.
3. The grain size analyses shows that domain-B has coarser grains of quartz than that in domain-A. This broader grain-size range decreased/delayed the effects of dislocation creep in domain B. Numerical models further indicate that, presence of coarser grains reduces the elastic strain energy density. These explain why the domain-B is devoid of P-planes in meso-scale.

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Appendix A. Supplementary data

Supplementary data related to this article can be found at <http://dx.doi.org/10.1016/j.jsg.2018.03.010>.

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